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**MATHEMATICAL LOGIC IN SLOVENIA 1960–2010**

**Abstract.** In the article the development of mathematical logic in Slovenia is explained. The main contributions of Slovenian logicians will be presented. Available courses and textbooks will be mentioned.

**Texts and courses available on mathematics departments**

Mathematical logic was introduced in Slovenia by Niko Prijatelj (1923–2003). In 1960 he published a book *Introduction to Mathematical Logic* [1]. This text covered propositional and predicate logic without model theory, so its content was less than usual introduction to mathematical logic. Zermelo–Fraenkel set theory was presented in his second book [2]. These texts have been used as introduction into foundation of mathematics on graduate level since 1968 on all mathematical studies in Slovenia. There were two exceptions. While preparing his new introductory books covering also model theory for predicate calculus and incompleteness of arithmetic [3–5] Prijatelj was giving 10 courses on Foundation of mathematics in interval 1982–1994. Andreja Prijatelj (1953–2002) gave similar courses on foundation of mathematics on Pedagogical Faculty in years 1997–2002. After the retirement of N. Prijatelj and premature death of A. Prijatelj mathematical logic on mathematical departments changed to contents from 1968.

The postgraduate study of mathematics in Slovenia was introduced in 1971. But only functional analysis was offered. Later some optional lectures could be chosen but not mathematical logic.

So almost all generations of Slovenian mathematicians have no formal education in mathematical logic although many of them have shown interest in it.

Some mathematicians changed to philosophy where they could get their thesis advisor or to computer science department. Of course this was not counted as mathematics. From 1980 study abroad has become possible, so many students not interested in functional analysis have gone abroad.

In 2010 new programs for mathematics include logic in its usual form (a century after *Principia mathematica*) and it is expected that the first student will receive Ph.D in mathematics with a thesis from logic.

**Researchers in mathematical logic**

In 1972 Boštjan Vilfan, whose advisor was Albert Meyer, received Ph.D from Massachusetts Institute of Technology for dissertation *The Complexity of Finite Functions*.

Vilfan was the advisor of Izidor Hafner, who after finishing postgraduate study of functional analysis got a doctorate with *thesis Theories of Lesniewski and their applications* on Faculty of electrical engineering and computing of University of Ljubljana in 1984.

Dana Scott from Carnegi Mellon [25] was advisor of Marko Petkovšek writing thesis *Finding closed-form solutions of difference equations by symbolic methods* in 1991.

In 1995 Andreja Prijatelj got Ph.D from Amsterdam University with dissertation *Investigating Bounded Contraction*. Advisors were A.S.Troelstra and J.F.A.K. van Benthem.

D. Scot was also the advisor of Andrej Bauer working on thesis *The realizability approach to computable topology and analysis* in 2000.

While Vilfan turned attention to programming and Petkovšek to computational mathematics, we are left with three logicians. Their works are mentioned in references. After finishing thesis Hafner has worked more on pedagogical aspects of logic, having an optional course of logic for computer science postgraduate students.

Andreja Prijatelj after organizing a solid basis for advance of Slovenian logic prematurely passed away and her logic pyramid collapsed in 2002.

So we are left with one promising working mathematical logician – A. Bauer.

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Mathematical Logic - books for free online reading: set theory, model theory, recursion theory, and proof theory. A Friendly Introduction to Mathematical Logic by Christopher C. Leary, Lars Kristiansen, 2015, 380 pp, 1.7MB, PDF. Fundamentals of Model Theory by William Weiss and Cherie D'Mello, 2000. The Game of Logic by Lewis Carroll, 1887. Logic for Computer Science Wikibooks, 2010, online html. Logic For Everyone by Robert A. Herrmann, 2006, 124 pages, 1MB, PDF. Logics of Time and Computation by Robert Goldblatt, 1992, 200 pages, 6.8MB, PDF. But, firstly, the advocate of mathematical reasoning in social science is not concerned to deny that mathematical reasoning in social, as well as in physical, science may be divested of symbol. Only it must be remembered that the question how far mathematics can with safety or propriety be divested of her peculiar costume is a very delicate question, only to be decided by the authority and in the presence of Mathematics herself. motion towards equilibrium is indeterminate, the position of equilibrium is mathematically determined. Examples not made to order, taken from the common stock of mathematical physics, will of course not fit so exactly. Publishes research papers on Mathematical Logic. Contributions from related areas are welcome. Addresses logicians and mathematicians, computer scientists, and philosophers interested in the applications of mathematical logic. 92% of authors who answered a survey reported that they would definitely publish or probably publish in the journal again. Journal information. Managing Editor.